



# Issuing GDP-linked bonds: demand and supply can match

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# Demand and supply – Government and investors

## Government

- What is the government's willingness to pay to insure its budget?
- What drives the stabilisation properties of GLBs, e.g. persistence.

## Investors

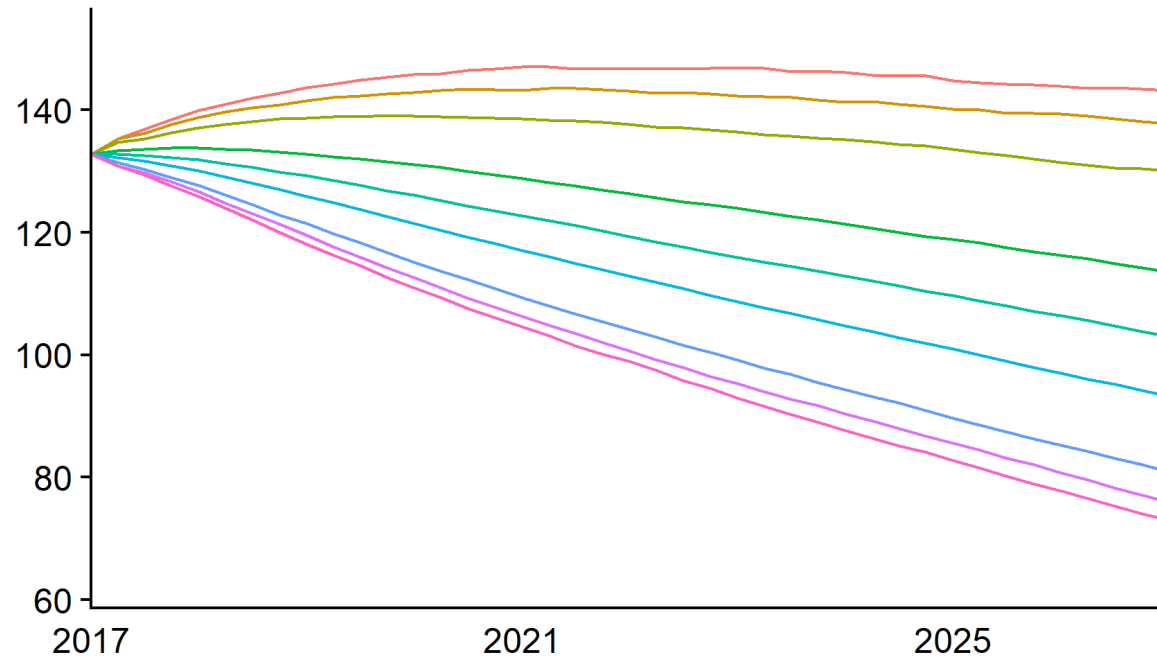
- What is the growth risk premium that investors will demand?
- Estimates from a CAPM taking persistence of shocks into account.



# Reduction of debt uncertainties

% of GDP

Italy: conventional debt



• **Conventional bonds:**

$$Var(\Delta d_t) = Var(pb_t) +$$

$$d_{t-1}^2 Var(r_t - g_t) -$$

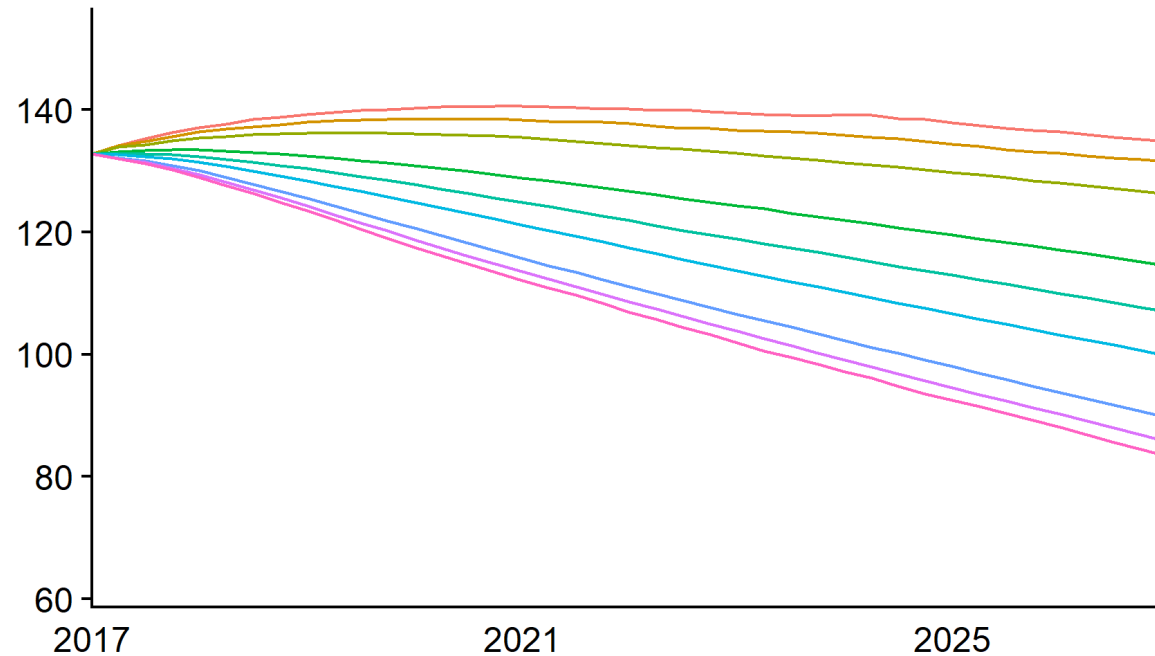
$$d_{t-t} Cov((r_t - g_t), pb_t)$$



# Reduction of debt uncertainties

% of GDP

Italy: GDP-linked debt

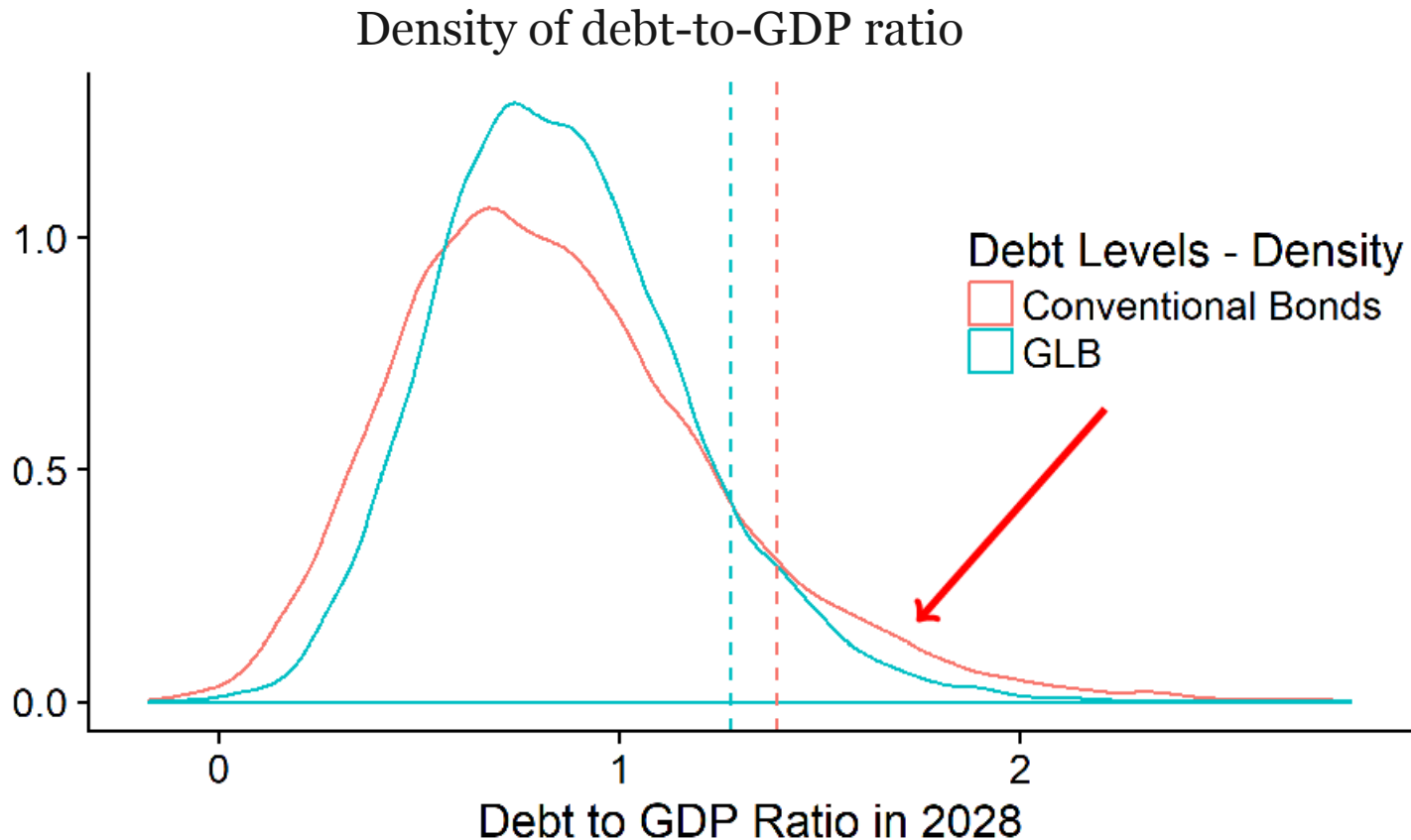


• **GDP linked debt :**

$$\text{Var}(\Delta d_t) = \text{Var}(pb_t)$$



# Insurance against tail events – an acceptable premium

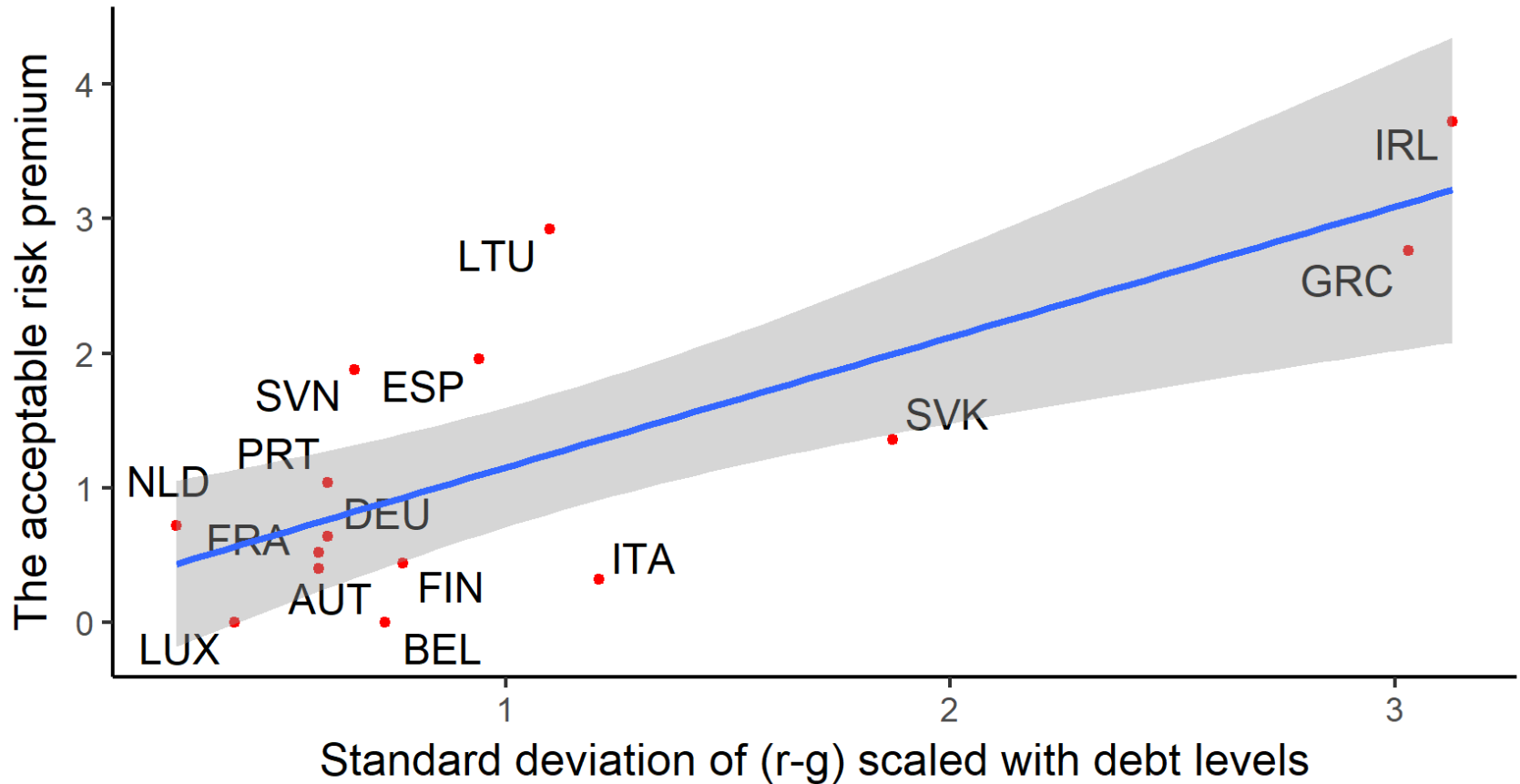


- Dashed lines at the 90<sup>th</sup> percentiles.
- What risk premium makes the two lines coincide?



# Stabilization effect: magnitudes and drivers

The acceptable premium and the standard deviation of  $(r-g) * \text{debt}$

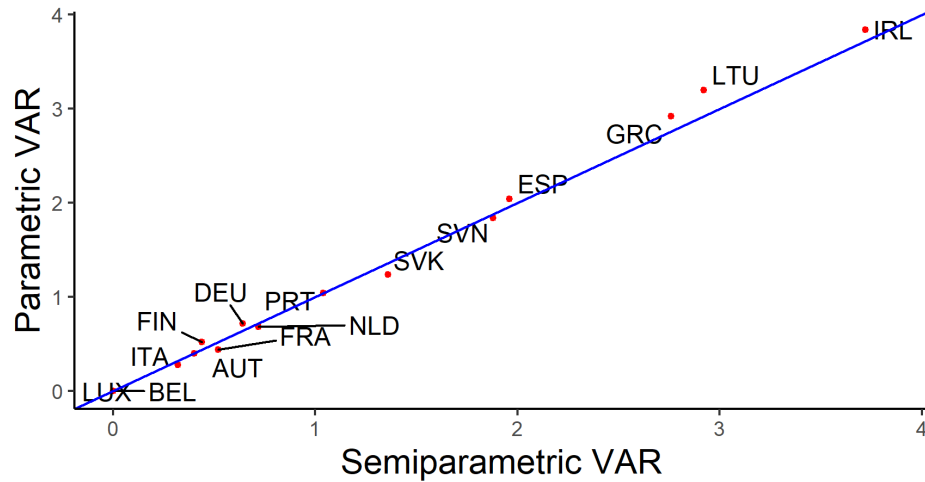


- The average of the acceptable premium is 1.25%.

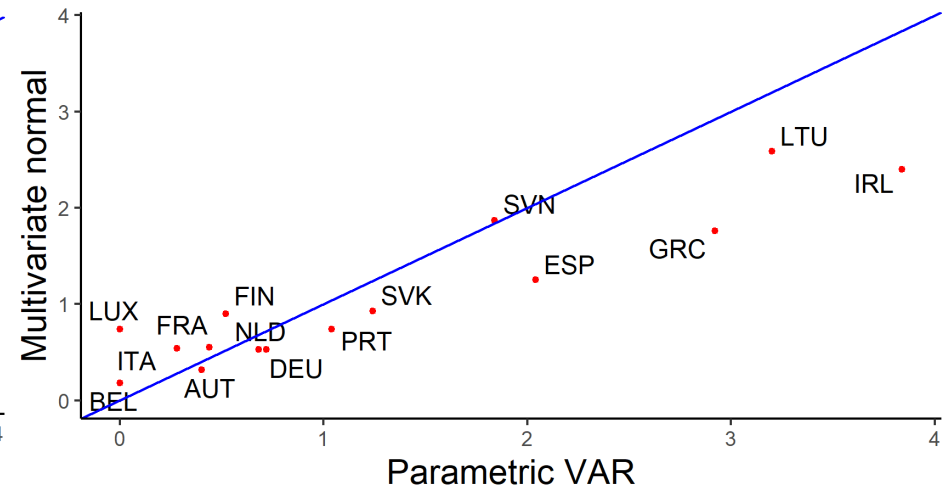


# Magnitudes and drivers of the premium

Acceptable risk premiums, baseline vs. parametric VAR



Acceptable Risk Premiums, VAR vs MVRN



- Persistence matters more than fat tails.



# Demand side: what risk premium compensates for GDP volatility

## Estimation steps

1

- Estimating the growth process (ARMA or VAR)

2

- Extracting the persistence factor and the innovation

3

- Calculating the risk premium (CAPM)





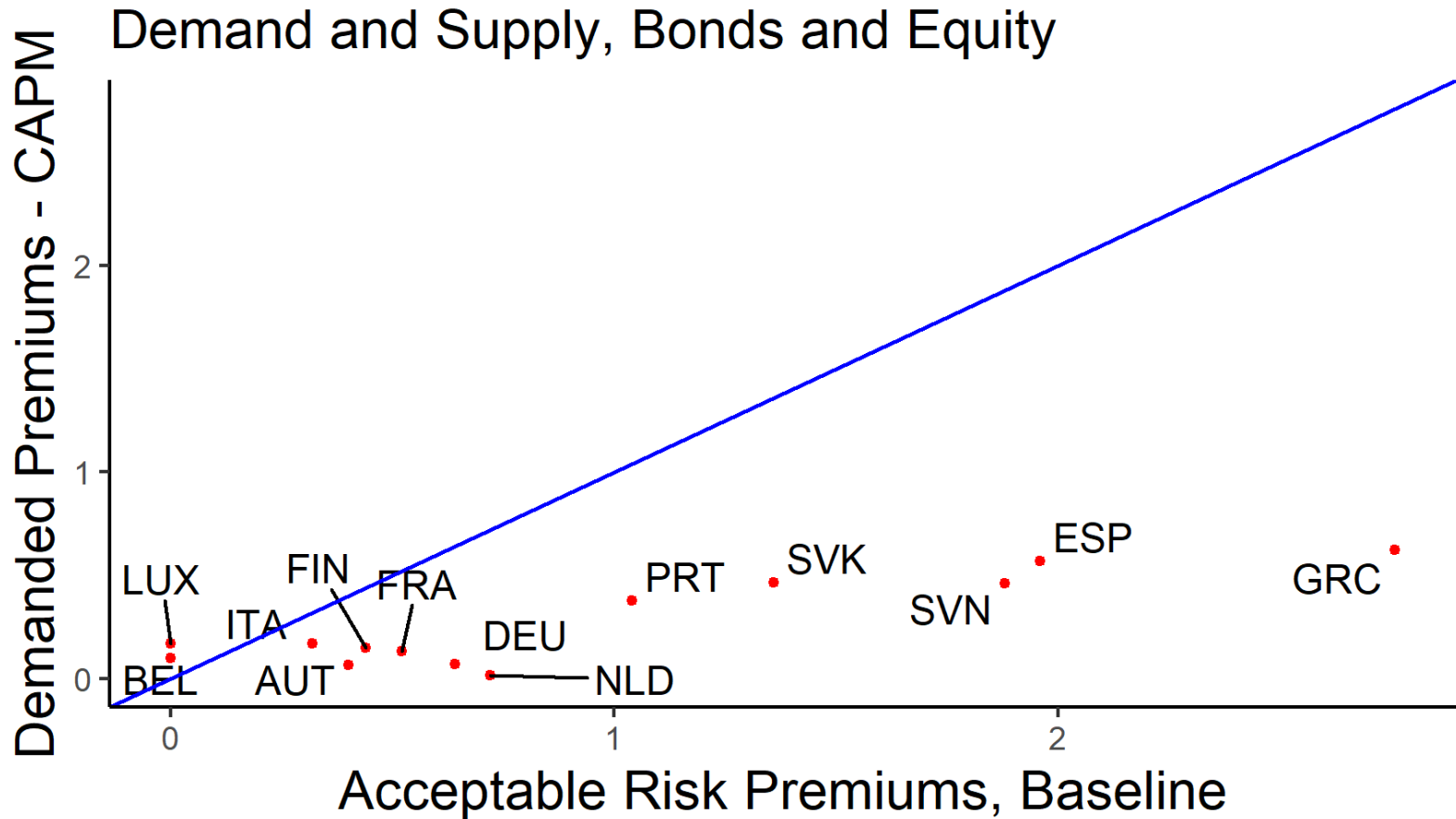
## Demand side: the return on a GLB

- The price of a GLB depends on the expected pay-off.
- The change of the price in each period reflects changes in the GDP forecast for all future periods  $k$ :  $E(g_k|I_t) - E(g_k|I_{t-1})$ .
- Thus the higher the persistence the higher the risk that is insured.
- For the CAPM this implies:

$$RP = (r_m - r_f) \frac{\text{Cov}\left(r_m, \frac{\sum_{k=t-1}^{+\infty} \frac{1}{(1+r)^{k-t}} (E(g_k|I_t) - E(g_k|I_{t-1}))V}{P_{t-1}}\right)}{\text{Var}(r_m)}$$



# The estimated premiums and the acceptable premiums





# Conclusion

- The persistence of shocks captured by a VAR structure matters.
- Persistence has also to be taken into account on the investor side: it increases the risk premium.
  - “There is more to insure”.
- The risk-premium that compensates for GDP volatility looks acceptable: this risk premium shifts the median debt level upwards but extremely high debt levels remain less likely.
- Government thus might want to “tap the market”.